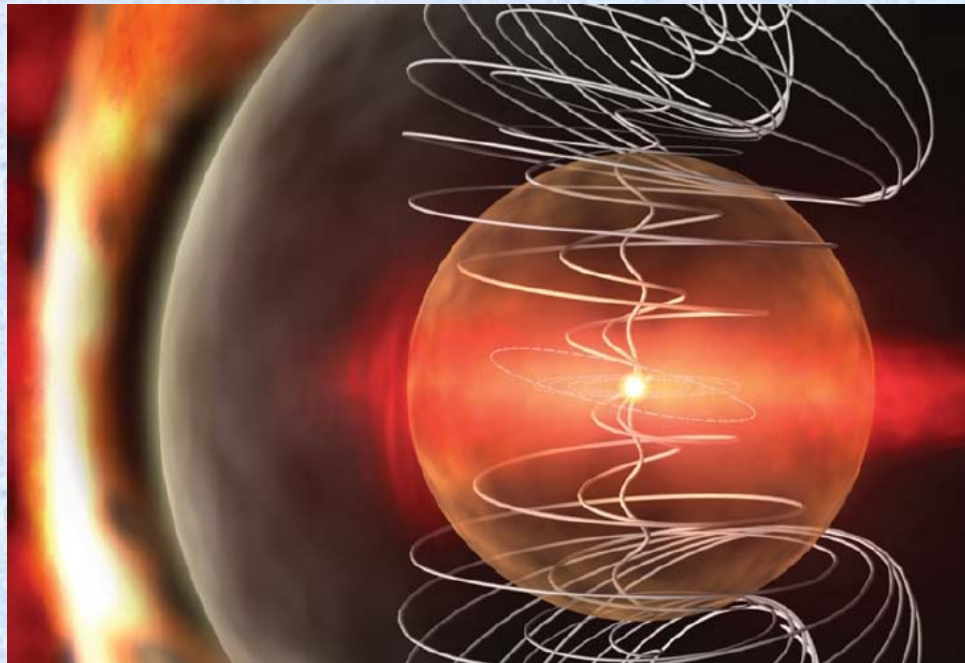


# La Heliosfera

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# Clase 2:

- La atmósfera solar
- El viento solar estacionario
  - La espiral de Parker
- Calentamiento local en el viento solar

# Static Corona (Chapman, 1957)

- Static, spherical symmetry
- Only force balance between gravity and fluid pressure
- Ideal Gas, isothermal
- $R$ =solar radius
- $p_0$ : pressure at solar surface
- $T \sim 10^6$  K

$$0 = -\frac{d}{dr} p - \rho \frac{GM_{solar}}{r^2}$$

$$\frac{1}{p} \frac{d}{dr} p = -\frac{Gm_p M_{solar}}{2kT} \frac{1}{r^2}$$

$$p(r) = p_0 \exp\left[-\frac{Gm_p M_{solar}}{2kT} \left(\frac{1}{r} - \frac{1}{R}\right)\right]$$

$$p(r) \xrightarrow{r \rightarrow \infty} p_0 \exp\left[-\frac{Gm_p M_{solar}}{2kTR}\right] \sim 3 \times 10^{-4} p_0$$

# Descubrimiento del **Viento Solar** (~50 años atrás)

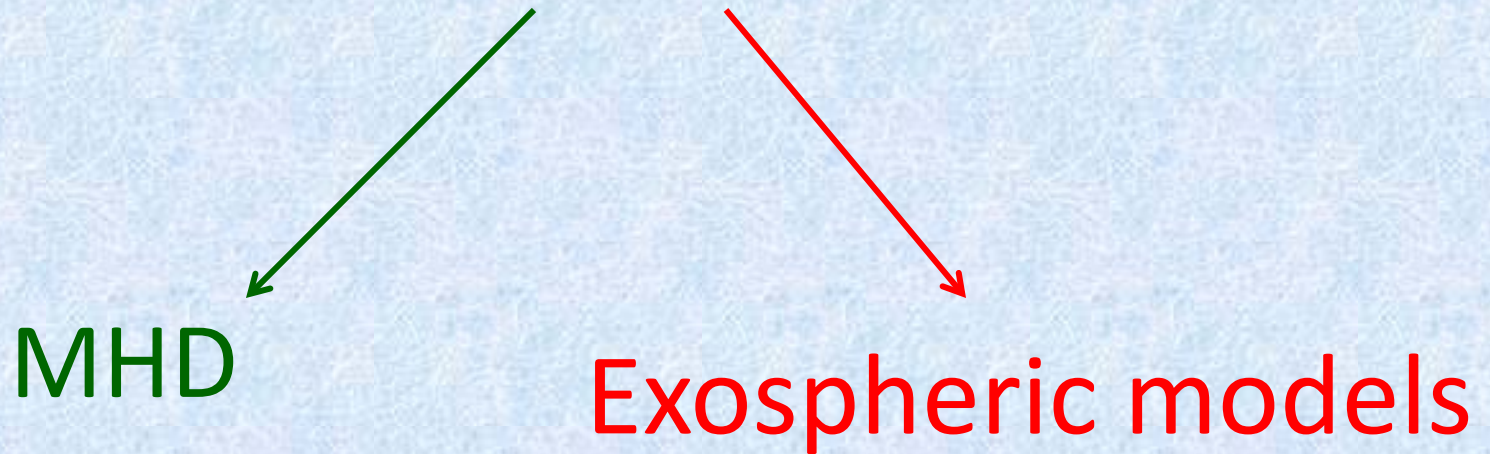
- Dirección 2<sup>da</sup> cola de cometas → anticipó viento solar
- Biermann (1951) estimó correctamente su velocidad (~ 400 km/s)
- Parker (1958) lo predijo teóricamente. Gravedad solar insuficiente para sostener atmósfera estática (**alta temperatura coronal**)
- En 1959 se observó por primera vez el viento solar con las sondas espaciales soviéticas Luniks



- $T \sim 10^5$  K → plasma (mayoría protones y electrones)
- 10 partículas por  $\text{cm}^3$  cerca de la Tierra
- Flujo de materia  $\sim 3 \times 10^9$  kg/seg  
(~ masa equivalente a la energía de fotones radiados)



# The Solar Wind



# Modelos exosféricos para el viento solar

- Gas en evaporación desde la corona solar
- Similar a exosfera terrestre (e.g.,  $\exists$  exobase), pero:  $\{g_S \gg g_T, T_{\infty S} \gg T_{\infty T}, \text{plasma no neutro}\}$
- Exobase ( $\lambda_{mfp} \sim H$ ):  $r_{exobase} \sim 3 R_S$

- Velocidad escape

$$v_{es}^p = \sqrt{g_S(r) r}$$

$$v_{es}^e \sim 43 v_{es}^p$$

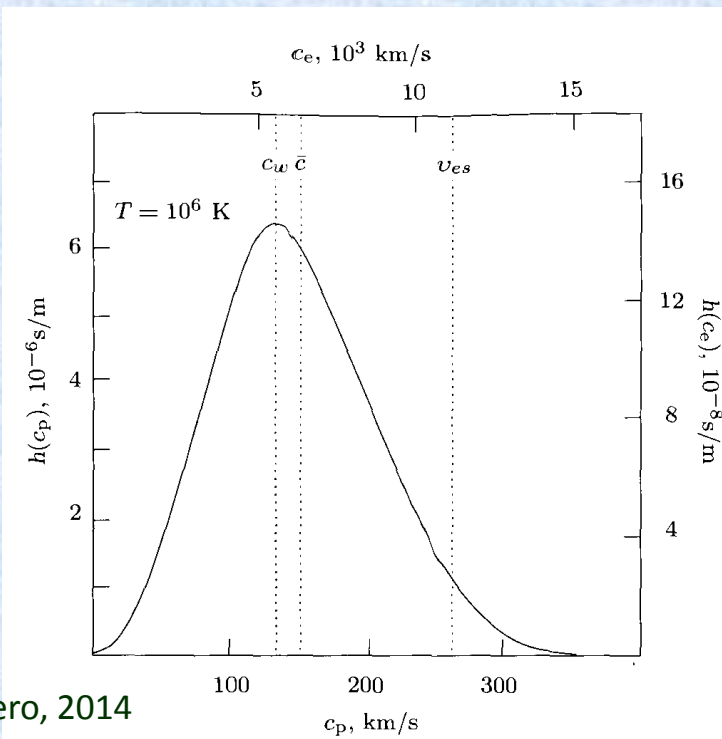
$$v_{es}^e = \sqrt{\frac{m_p}{m_e}} v_{es}^p$$

- La diferencia entre  $v_{es}^e$  y  $v_{es}^p$  produciría Sol con carga + (**E**)

(e- escapan mas rápido que p+ !!!)

Entonces el campo **E** de polarización:

Frena e- y acelera p+



# Modelo de Parker: Viento Solar radial estacionario isotérmico

Conservación masa

$$\frac{\partial}{\partial t} \rho + \nabla \cdot (\rho \mathbf{U}) = 0$$

$$r^2 \rho(r) U(r) = A$$

Conservación momento (desprecio fuerza magnética, ya que B es radial cerca del Sol y la inercia gana lejos del Sol )

$$\rho \frac{D}{Dt} \mathbf{U} = -\nabla p + \mathbf{J} \times \mathbf{B} - \frac{\rho GM_{Sun}}{r^2} \hat{\mathbf{r}} + \rho \mathbf{F}$$

$$U \frac{d}{dr} U = -\frac{1}{\rho} \frac{d}{dr} p - \frac{GM_{Sun}}{r^2}$$

Gas ideal isotérmico

$$pV = \sum_j^{especies} N_j k_B T_j = (N_p + N_e) k_B T = 2N k_B T$$

$$\frac{dp}{dr} = 2k_B T \frac{dn}{dr}$$

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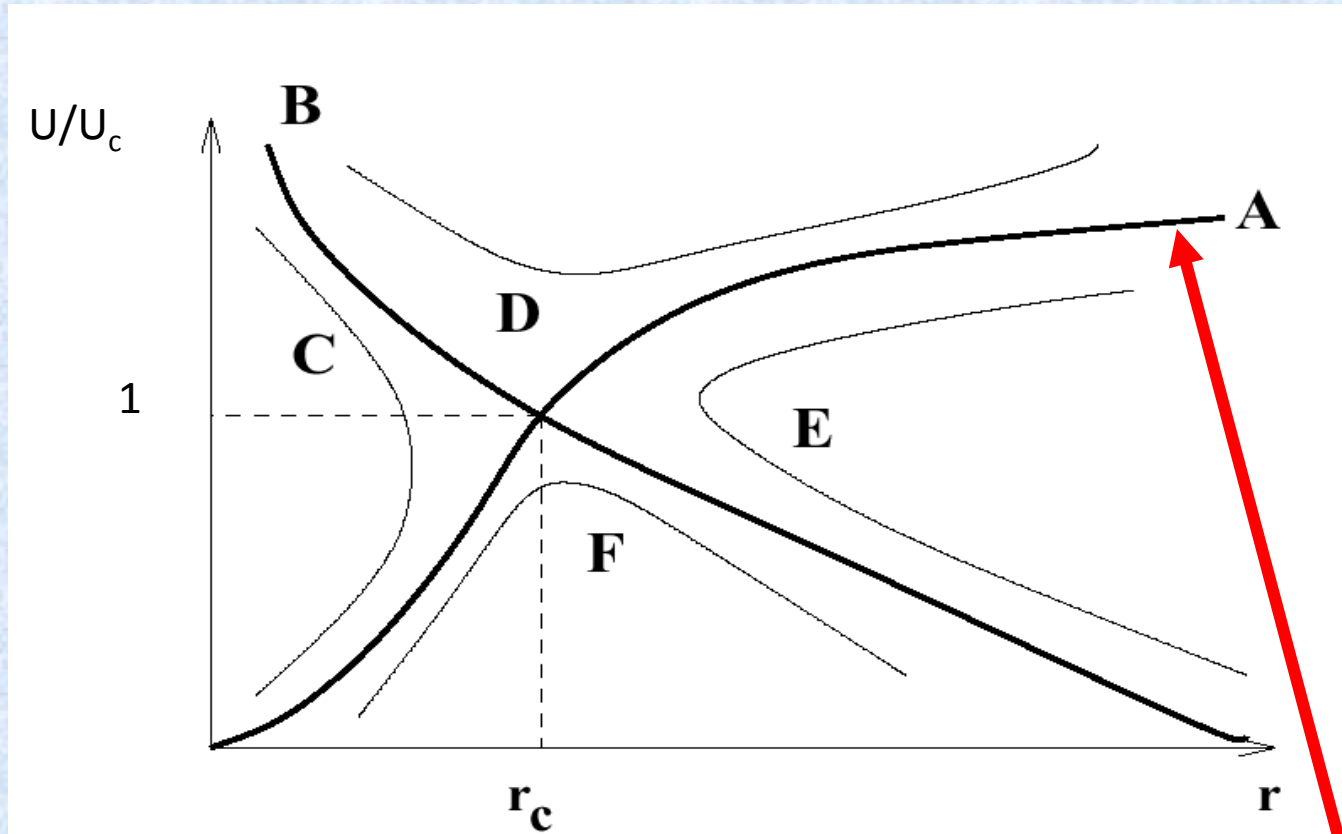
$$UU' - 2k_B T (2U + rU') + \frac{GM_{Sun}}{r^2} = 0$$

$$r_c = \frac{GM_{Sun} m_H}{4k_B T} \quad (\text{critical point})$$

$$\ln(U^2 / U_c^2) - \frac{U^2}{U_c^2} + 4 \left( \frac{r_c}{r} + \ln(r / r_c) \right) = C$$

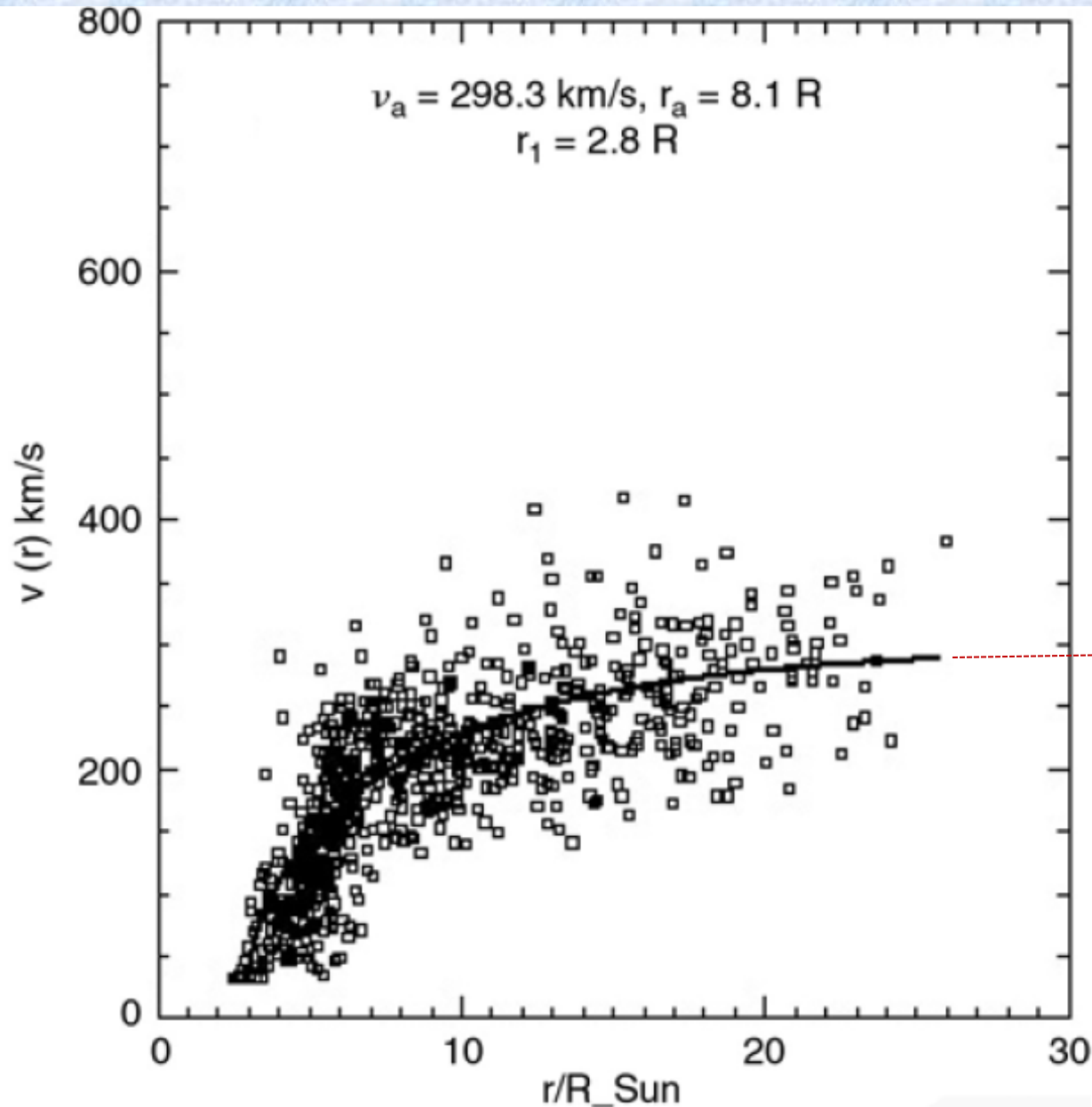
$$U_c \doteq U(r_c) = \sqrt{\frac{2k_B T}{m_H}} \quad (\text{critical speed})$$





- Manifold of solutions
- $U$  monotonically from sub-sonic to super-sonic in SW  $\rightarrow$  branch **A**
- For the SW:  $r_c \sim 10 R_{\text{Sun}} \sim 0.05 \text{ AU}$
- $U \rightarrow \text{constant}$  for  $r \gg r_c$

# Observed profile of SW speed



Observations  
(difference images from  
SOHO LASCO)  
of plasma traces

Fitted model given by  
Sheeley et al.[1997]

Figure from  
McComas et al.,  
Rev. of Geophysics [2007]

Velocities in agreement  
with in situ observations  
(Helios S/C) near 0.3 AU

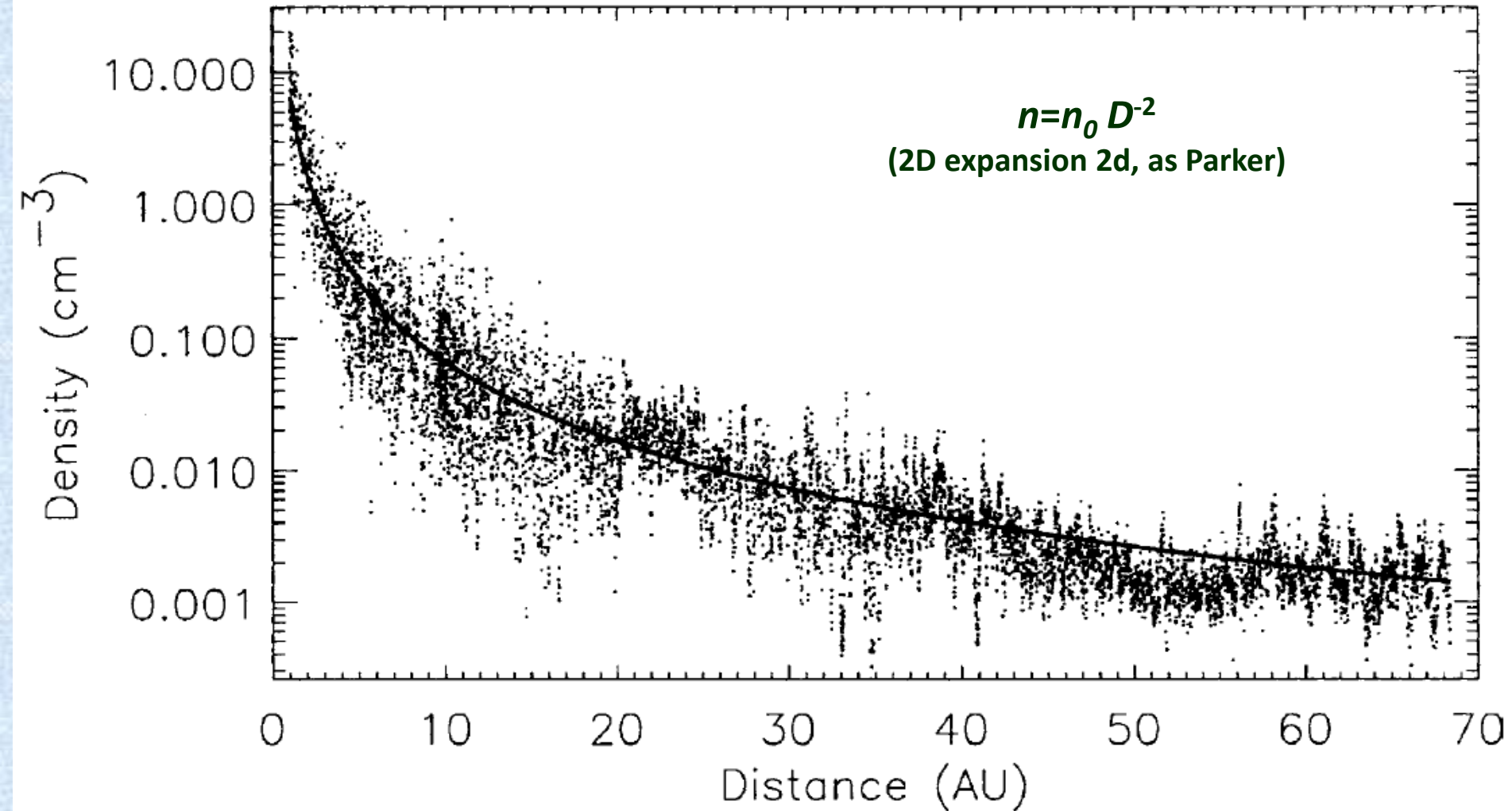
# Stationary simplified Solar Wind

Assuming  $V_r = \text{cte}$  (2D expansion)

Conservation of mass  $\rightarrow n_p \sim D^{-2}$

[From Richardson et al., ASR, 2004]

Observations from Voyager



# Stationary simple Solar Wind at ecliptic

## Assuming ideal MHD and $V_r = \text{constant}$

Conservation of magnetic flux in an elementary fluid parcel

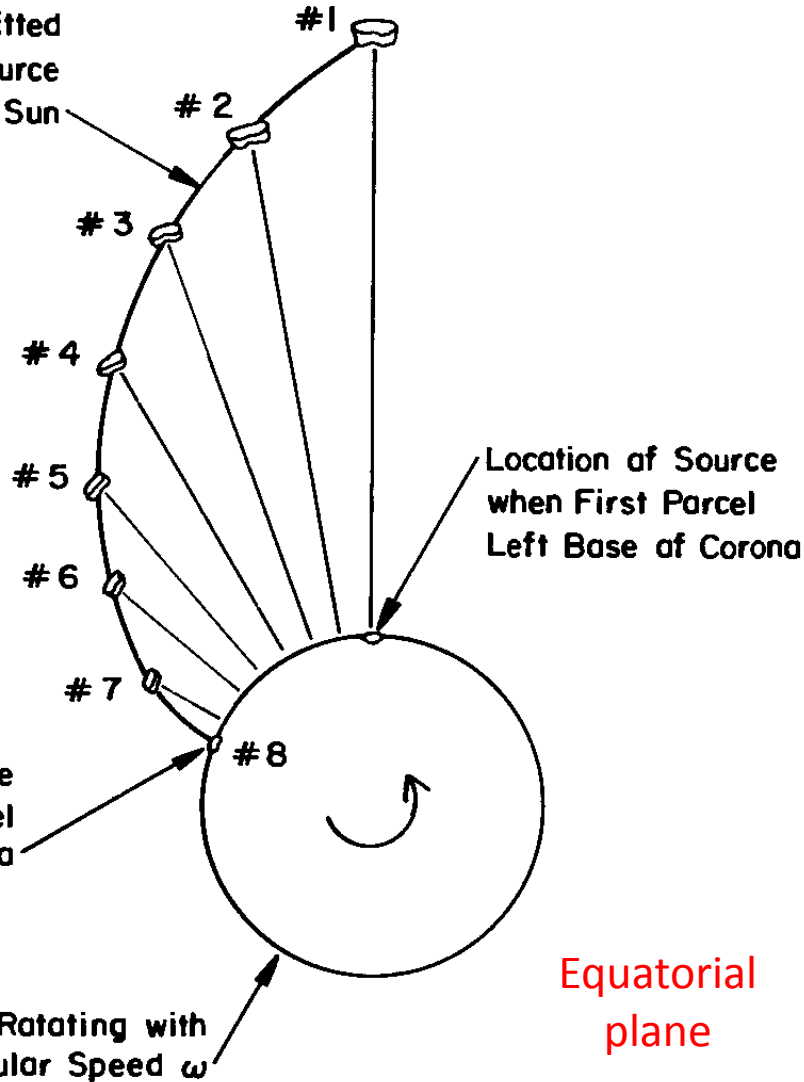
$$\rightarrow B_r \sim D^{-2} \quad \& \quad B_\phi \sim D^{-1}$$

$$\text{Then } B \sim \sqrt{D^{-2} + D^{-1}}$$

angle ( $\mathbf{B}$ , radial from Sun):  $\tan(\alpha) = B_\phi / B_r \sim D$

Note that at ecliptic plane  $B_z \sim 0$

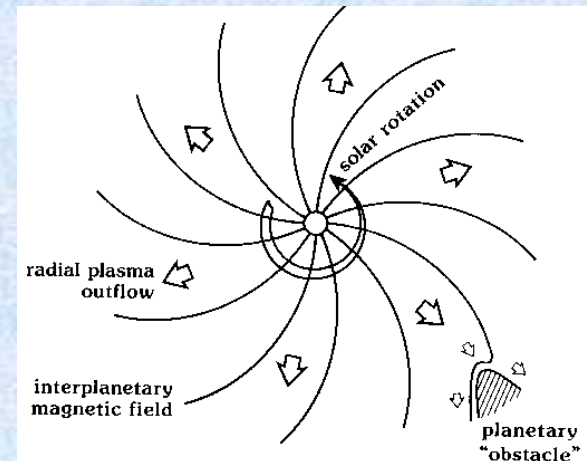
Spiral Locus of Fluid Parcels Emitted from a Fixed Source on Rotating Sun



## Parker Spiral from:

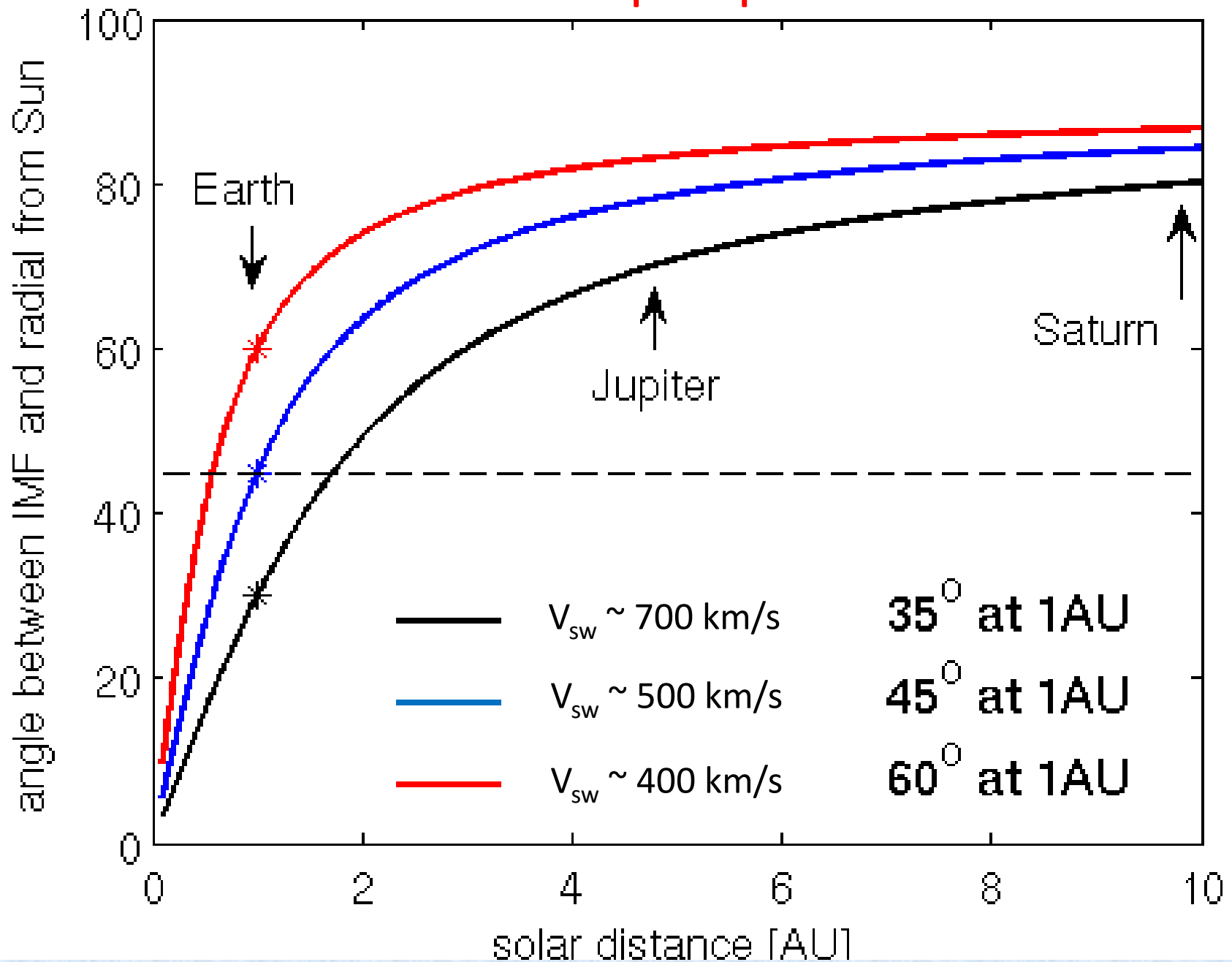
- Solar rotation
- Radial flow
- 'Frozen-in' condition

$\alpha \sim 45^\circ$  for 1AU



$$\frac{B_\phi}{B_r} = \tan(\alpha) = \frac{\Omega D}{U_{sw}}$$

# At the ecliptic plane

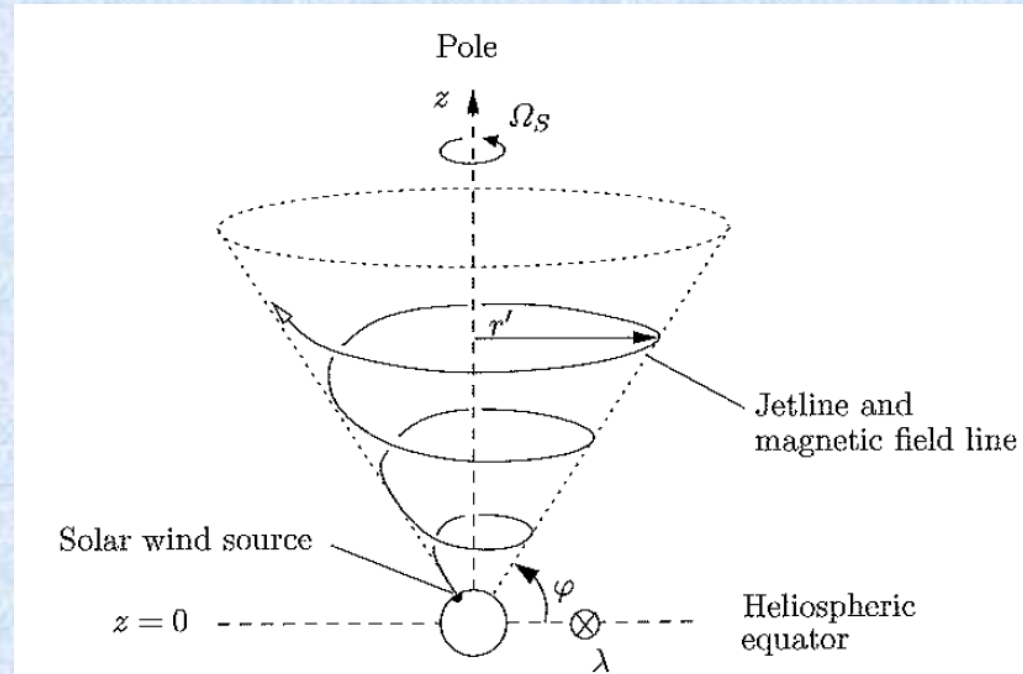


# Interplanetary Magnetic Field (3D) in stationary Solar Wind (simple model)

$$\mathbf{B} = B_r(r)\hat{\mathbf{r}} + B_\lambda(r)\hat{\boldsymbol{\lambda}}$$

$$B_r(r) = B_0 \left(\frac{r_0}{r}\right)^2$$

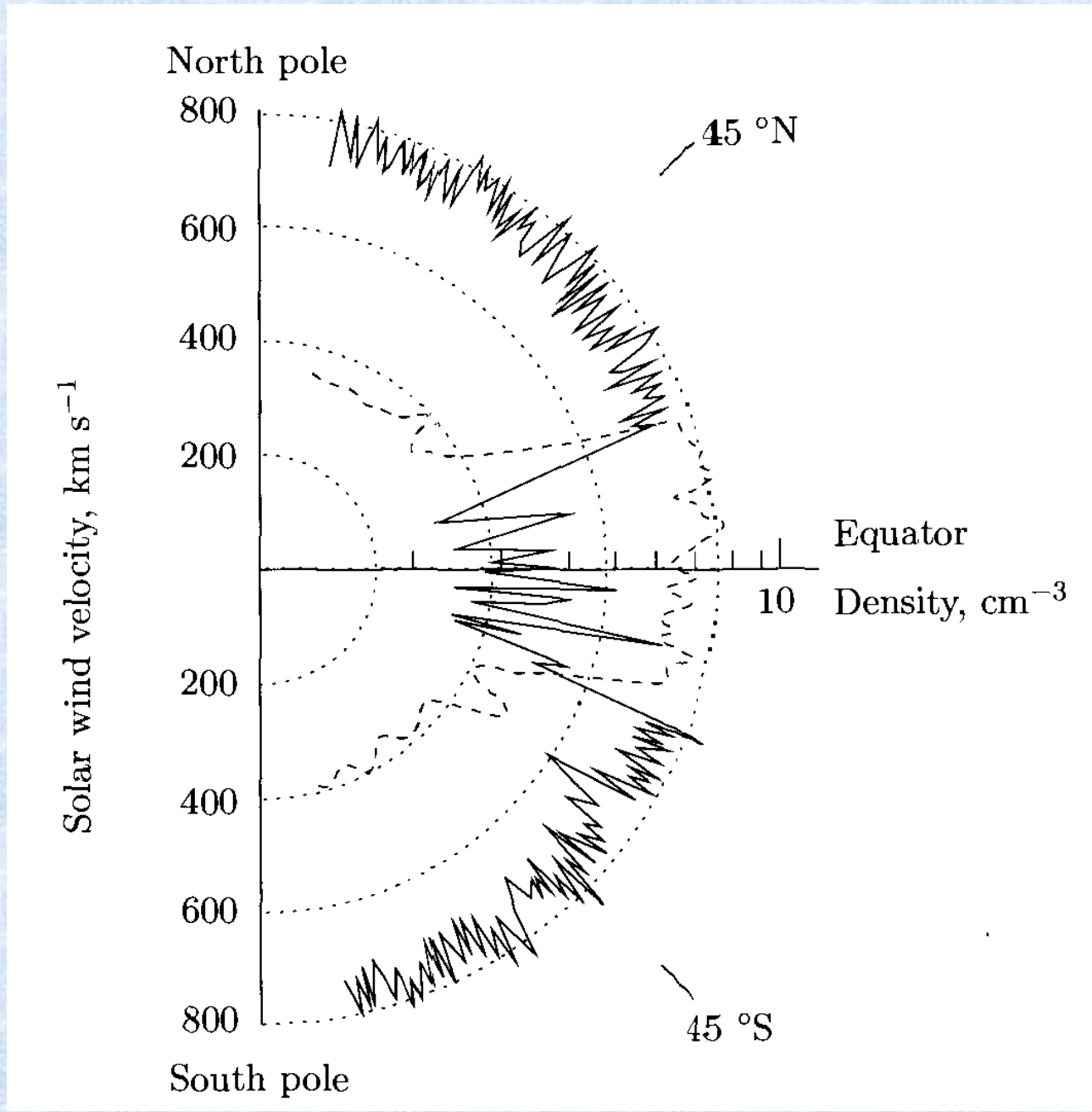
$$B_\lambda(r) = -B_0 \frac{r_0 \Omega_{Sun}}{U_{sw}} \left(\frac{r_0}{r}\right) \cos(\varphi)$$



$$B(r) = B_0 \left(\frac{r_0}{r}\right)^2 \sqrt{1 + \frac{r^2 \Omega_{Sun}^2 \cos^2(\varphi)}{U_{sw}^2}} \xrightarrow{r \gg 1AU} \frac{B_0 r_0^2 \Omega_{Sun} \cos(\varphi)}{r U_{sw}}$$



Estructura  
del Viento  
solar en  
latitud:  
viento rápido  
y  
viento lento



# Differences of **Slow** and **Fast** SW properties

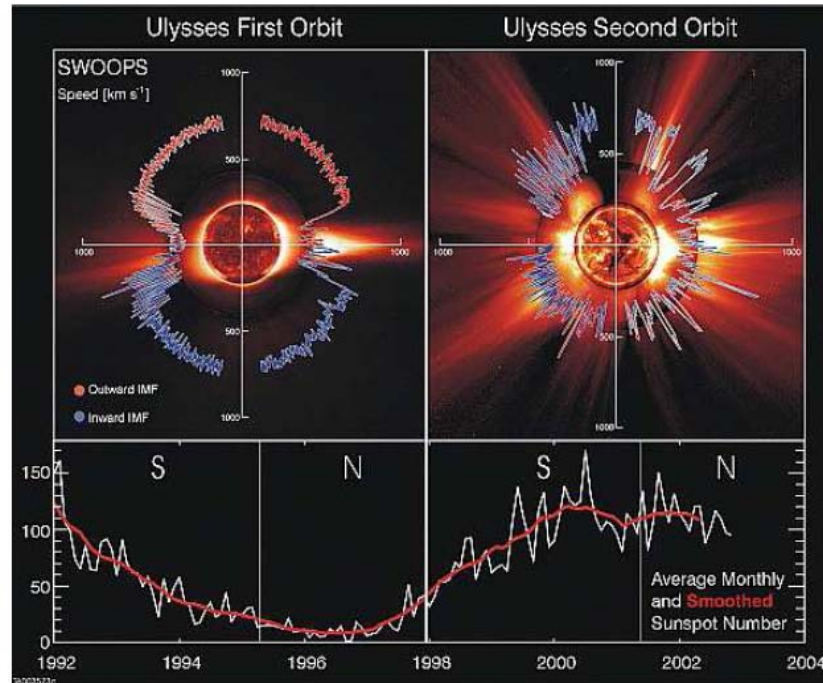
## Slow SW

$v \sim 250 - 400 \text{ Km/s}$   
 $n \sim 10 - 40 \text{ cm}^{-3}$   
 $T \sim 10^3 - 10^4 \text{ }^\circ\text{K}$

- Higher density
- Cooler

- Lower level of fluctuations
- $\delta \mathbf{b}$  poorly correlated with  $\delta \mathbf{u}$ 
  - Fluctuations of  $\delta \rho$
- (but incompressibility remains as good assumption)
- High level of  $\delta |\mathbf{b}|$  ( $\delta |\mathbf{b}| \sim B_0$ )

From [McComas et al., 2003]



## Fast SW

$v \sim 600 - 800 \text{ Km/s}$   
 $n \sim 1 - 4 \text{ cm}^{-3}$   
 $T \sim 10^4 - 10^5 \text{ }^\circ\text{K}$

- Lower density
- Hotter

- Higher level of fluctuations
  - High level of  $\delta \mathbf{b}$  and  $\delta \mathbf{u}$  ( $|\delta \mathbf{b}| \sim B_0$ ,  $|\delta \mathbf{u}| \sim U_0$ )
  - $\delta \mathbf{b}$  highly correlated with  $\delta \mathbf{u}$
  - Low level of  $\delta \rho$  ( $\delta \rho \ll \rho_0$ )
  - Low level of  $\delta |\mathbf{b}|$  ( $\delta |\mathbf{b}| \ll B_0$ )

# Modelo dinámico para flujo de Viento Solar

Conservación de la masa  
(Ley de Lavoisier)

$$\frac{\partial}{\partial t} \rho + \nabla \cdot (\rho \mathbf{U})$$

Conservación del momento lineal  
(2<sup>da</sup> ley de Newton)

$$\rho \frac{D}{Dt} \mathbf{U} = -\nabla p + \mathbf{J} \times \mathbf{B} - \frac{\rho GM_{Sun}}{r^2} \hat{\mathbf{r}} + \rho \mathbf{F}$$

Conservación de la energía interna,  
aplicada a un elemento de fluido  
(1<sup>era</sup> ley de la termodinámica)

$$\frac{D}{Dt} \delta E = -p \frac{D}{Dt} \delta V + \delta M Q - \delta V \nabla \cdot \mathbf{q}$$

# Modelo radial para Viento Solar estacionario

Conservación masa

$$r^2 \rho(r) U(r) = c$$

Conservación momento (desprecio fuerza magnética, ya que B es radial cerca del Sol y la inercia gana lejos del Sol )

$$U \frac{d}{dr} U = -\frac{1}{\rho} \frac{d}{dr} p - \frac{GM_{Sun}}{r^2} + F_r$$

Conservación energía

$$E = \frac{f \rho k_B T \delta V}{2\mu}, \quad p = \frac{\rho k_B T}{\mu}, \quad \mu = \frac{\sum n_i m_i}{\sum n_i}$$

$$\frac{f}{2} \frac{d}{dr} T - T \frac{d}{dr} \ln(\rho) = \frac{\rho}{T^{f/2-1}} \frac{d}{dr} \left( \frac{T^{f/2}}{\rho} \right) = \frac{\mu}{k_B} \left( \frac{Q}{U} - \frac{d}{dr} \left( \frac{q}{\rho U} \right) \right)$$

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# Viento Solar Esférico, radial, estacionario, $U=U_0$

Conservación masa

$$\rho(r) = c r^{-2}$$

Conservación momento lineal

$$-\frac{1}{\rho} \frac{d}{dr} p - \frac{GM_{Sun}}{r^2} + F_r = 0$$

Conservación energía: perfil  $T(r)$

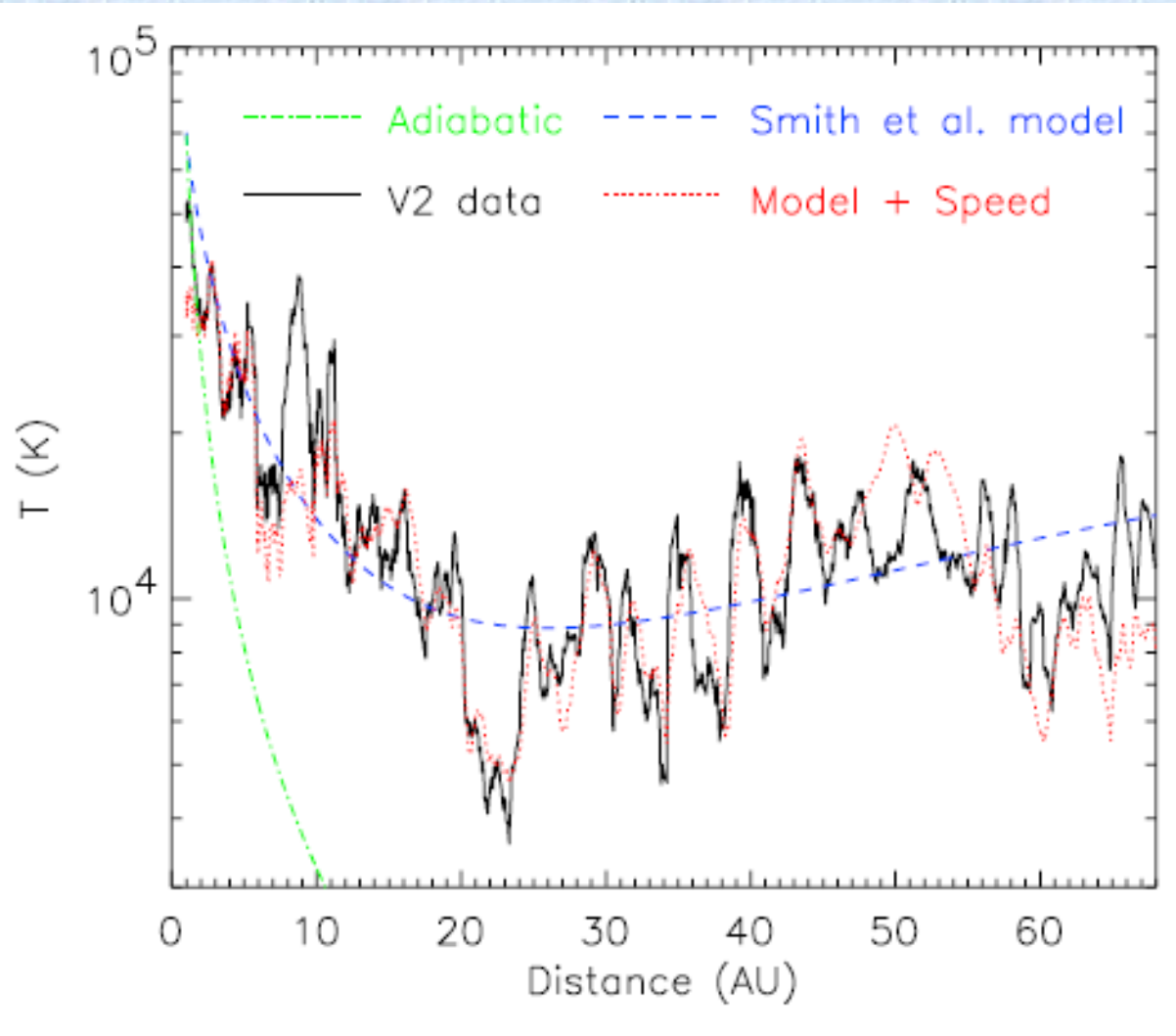
$$\frac{r^{-2}}{T^{f/2-1}} \frac{d}{dr} \left( \frac{T^{f/2}}{r^{-2}} \right) = \frac{\mu}{k_B} \left( \frac{Q}{U} - \frac{d}{dr} \left( \frac{q}{c r^{-2} U} \right) \right)$$

Sin flujo de calor ni calentamiento ( $q=0=Q$ )

(3 grados de libertad por partícula:  $f=3$ )

$$\frac{r^{-2}}{T^{f/2-1}} \frac{d}{dr} \left( \frac{T^{f/2}}{r^{-2}} \right) = 0 \longrightarrow T(r) = T_0 \left( \frac{r}{r_0} \right)^{-4/3}$$

# Local heating in the Solar Wind



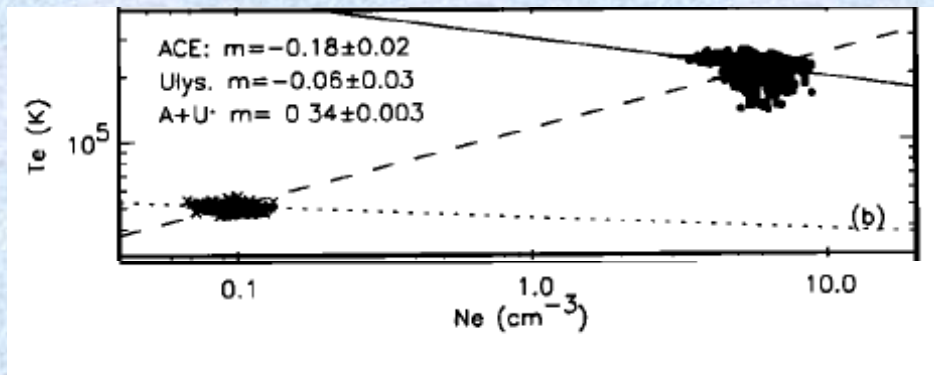
Presence of Turbulence in SW:  
Turbulent dissipation !!

[From Richardson & Smith, GRL, 2003]

# Multi-spacecraft study of one single MC

For a perfect gas  $T \sim N^{\gamma-1}$  ( $\gamma$  the polytropic index, associated with heating of the gas)  
 $\gamma=1 \rightarrow$  isothermal expansion &  $\gamma=5/3 \sim 1.67 \rightarrow$  adiabatic expansion

From observations of the same MC (March 1998)  
at 1AU (ACE) and  $\sim 5$  AU (Ulysses), possible to get an  
estimation of  $\gamma$



$$T_e \sim N_e^{0.34} (\gamma \sim 1.34)$$

A very different result from a  
non-correct estimation of  $\gamma$   
using single S/C observations

[From Skoug et al., JGR 2000]

However, a real theoretical approach needs  
more ingredients (e.g., kinetic effects and  
anomalous heat fluxes)



**Fin clase 2**